**Pearson/Edexcel**

**GCSE (9-1) Mathematics (1MA1)**

**Problem-solving questions 4**

**Foundation Tier**

**Time: 1 hour 30 minutes**

You should have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Calculator permitted

Calculator not permitted in questions with \*

**1.** The diagram shows an edge of a cliff, *AD*, with a zip line, *AB*.

*A*

*B*

*C*

*D*

*E*

 29 m

2°

 14 m

The time taken for Tom to travel down the zip line, *AB*, is 19 seconds.

(a) Work out the length of *AB*.

**(1)**

(b) Work out Tom’s average speed, in m/s, to travel down the zip line, *AB*.

Give your answer correct to 3 significant figures.

**(2)**

**(Total for question 1 is 3 marks)**

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**2\*.** *ABC* is a triangle with vertices *A*(1, −4), *B*(−5, 2) and *C*(11,6).

*M* is the midpoint of *BC*.

The line *L* passes through M and is perpendicular to *AC*.

(a) Work out the midpoint of

(i) *BC*,

(ii) *AC*.

**(1)**

(b) Work out the gradient of the line

(i) joining M to the midpoint of *AC*,

(ii) *AC*.

**(2)**

(c) Show that the line *L* passes through the midpoint of *AC*.

**(1)**

**(Total for question 2 is 4 marks)**

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**3\*.** f and g are functions such that

 f(*x*) = 2*x* – 3 g(*x*) = *x*2 – 4

(a) Find gf(*x*) in the form (*ax* + *b*)2 + *c*.

**(1)**

(b) Find gf(*x*) in the form *ax*2 + *bx* + *c*.

**(1)**

(c) Given that h(*x*) = gf(*x*), express h(*x*) in the form *p*(*x* + *q*)2 + *r*.

**(2)**

(d) State the coordinates of the turning point of the graph with equation h(*x*).

**(1)**

**(Total for question 3 is 5 marks)**

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**4.** Mary sells sausage rolls in her shop.

The number of sausage rolls sold on Friday is *x*.

On Saturday she sold 20% more sausage rolls than on Friday.

On Sunday she sold 25% fewer sausage rolls than on Saturday.

(a) Write down an expression, in terms of *x*, of the number of sausage rolls sold on Saturday.

**(1)**

(b) Write down an expression, in terms of *x*, of the number of sausage rolls sold on Sunday.

**(1)**

On Sunday she sold 81 sausage rolls.

(c) Write down an equation, in terms of *x*, for the number of sausage rolls sold on Sunday.

**(1)**

(d) Work out the total number of sausage rolls sold on Friday, Saturday and Sunday.

**(1)**

**(Total for question 4 is 4 marks)**

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**5\*.** The diagram shows the graph of *y* = −4*x* + *c*

*y*

*x*

*c*

× (2, 10)

× (4, *a*)

(a) Work out the value of *c*.

**(2)**

(b) Work out the value of *a*.

**(2)**

**(Total for question 5 is 4 marks)**

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**6\*.** A box contains apples.

The total number of apples in the box is *x*.

There are three times as many red apples as green apples in the box.

  of the red apples are rotten.

  of the green apples are rotten.

(a) (i) Write down the proportion of red apples, in terms of *x*, in the box.

 (ii) Write down the proportion of green apples, in terms of *x*, in the box.

(b) (i) Write down the proportion of rotten red apples, in terms of *x*, in the box.

 (ii) Write down the proportion of rotten green apples, in terms of *x*, in the box.

**(1)**

The number of rotten apples in the box is 35

(c) (i) Write down an expression, in terms of *x*, of the total number of rotten apples.

 (ii) Write down an equation, in terms of *x*, of the total number of rotten apples.

**(1)**

(d) Work out the total number of apples in the box.

**(2)**

**(Total for question 6 is 4 marks)**

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**7.**

*A*

*B*

*C*

*D*

*E*

10.4 m

65°

9.2 m

*ABE* and *DCE* are congruent triangles.

*BEC* is a sector of a circle with centre *E*.

*AB* = 10.4 m

*AE* = 9.2 m

Angle *BEC* = 65°

The area of sector *BEC* = 80 m2.

(a) Work out the radius of the sector *BEC*.

**(2)**

(b) Work out the size of angle *BAE*.

**(1)**

(c) Work out the area of triangle *BAE*.

**(1)**

(d) Work out the total area of the two triangles.

**(1)**

**(Total for question 7 is 5 marks)**

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**8.** The diagram shows a rectangular label taken off a cylindrical tin.

11 cm

24 cm

 cm

The label covers the curved surface of the tin with no overlap.

(a) Work out the diameter of the tin.

**(1)**

(b) Work out the radius of the tin.

**(1)**

(c) Work out the volume of the cylindrical tin.

 Give your answer correct to 3 significant figures.

**(2)**

**(Total for question 8 is 4 marks)**

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**9\*.** There are 315 counters in a box.

There are only red counters, green counters and blue counters in the box.

The ratio of the number of red counters to the number of green counters is 4 : 3

The ratio of the number of green counters to the number of blue counters is 2 : 7

(a) Write down the ratio of the number of red counters to the number of green counters to the number of blue counters.

**(2)**

(b) Work out the number of

(i) red counters,

(ii) blue counters.

**(1)**

(c) Work out the difference between the number of red counters and the number of blue counters.

**(1)**

**(Total for question 9 is 4 marks)**

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**10\*.** Here are two sheets of cards.

 Card *X* (labelled *ABCD*) and card *Y* (labelled *EFGH*)are parallelograms.

**Card *Y***

*F*

*G*

**Card *X***

*E*

(2*x* − 1) m

*A*

*B*

*C*

*D*

(*x* + 1) m

*H*

Card *X* has height (*x* + 1) m and area 4 m2.

Card *Y* has height (2*x* – 1) m and area 6 m2.

(a) (i) Write down an expression, in terms of *x*, for the length *AD*.

 (ii) Write down an expression, in terms of *x*, for the length *EH*.

**(1)**

The sum of length *AD* and length *EH* is 8 m.

(b) Write down an equation, in terms of *x*, for the sum of length *AD* and length *EH*.

**(1)**

(c) Write the equation in the form *ax*2 + *bx* + *c* = 0

**(1)**

(d) Solve the equation *ax*2 + *bx* + *c* = 0

**(1)**

(e) Work out the length of *AD* and the length of *EH*.

 You must show your working.

**(2)**

**(Total for question 10 is 6 marks)**

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**11.** *ABD* and *BDC* are triangles.

*A*

*B*

*C*

*D*

38°

56°

47°

24 cm

17 cm

(a) Work out the length of *BD*.

**(2)**

(b) (i) Work out the size of the angle *BAD*.

 (ii) Work out the length of *AD*.

**(1)**

(c) Work out the area of triangle *ABD*.

 Give your answer correct to 3 significant figures.

**(2)**

**(Total for question 11 is 5 marks)**

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**12.** . The speed-time graph shows the speed of a car during the first 90 seconds of a journey.

Time (seconds)

0

20

40

60

80

100

Speed (m/s)

The car accelerates, then travels at a steady speed of *v* m/s and then decelerates.

(a) Write down the area under the graph in terms of *v*.

**(2)**

The total distance travelled by the car in the first 90 seconds is 2.08 km.

(b) Write down an equation, in terms of *v*, for the area under the graph.

**(1)**

(c) Work out the value of *v* in m/s.

**(1)**

**(Total for question 12 is 4 marks)**

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**13\*.** Here is a number grid with a shaded T-shape.

The T-shape can be translated in any direction on the grid.

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |

(a) (i) Complete the T-shape.

*n*

*………*

*………*

*………*

*………*

 (ii) Write down the sum of the T-shape, in terms of *n*, in simplified form.

**(2)**

(b) Prove algebraically that the sum of the numbers in any of these translated T-shapes is a multiple of 5

**(1)**

**(Total for question 13 is 3 marks)**

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**14\*.** The diagram shows a sheet of metal.

*A*

*B*

*C*

*D*

*E*

*F*

*G*

*H*

*I*

*J*

3 cm

(*x* + 1) cm

*ABCJ*, *GHIJ* and *CDEF* are squares.

*JCFG* is a rectangle.

*GH* = *FE*

*ED* = 3 cm

*AB* = (*x* + 1) cm

(a) Work out the area of

(i) *CDEF*,

(ii) *JIHG*.

(b) Work out the area, in terms of *x*,of

(i) *JCFG*,

(ii) *ABCJ*.

**(1)**

The total area of the sheet of metal is 88 cm2

(c) Write down an equation, in terms of *x*, of the sheet of metal in the form *ax*2 + *bx* + *c* = 0

**(2)**

(d) Work out the value of *x*.

 You must show your working.

**(2)**

**(Total for question 14 is 5 marks)**

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**15\*.** Here is a rectangle *ABCD* and a triangle *EFG*.

*A*

*B*

*C*

*DA*

cm

cm

*E*

*F*

*G*

cm

*h* cm

(a) Work out that area of rectangle *ABCD*.

(b) Write down an expression, in terms of *h*, of the area of triangle *EFG*.

The area of triangle *EFG* is twice the area of rectangle *ABCD*.

(c) Write down an equation in terms of *h*.

**(1)**

(d) Make *h* the subject of the equation.

**(1)**

(e) Work out the height, *h* cm, of triangle *DEF*.

 Give your answer in the form  where *a* and *b* are integers.

**(2)**

**(Total for question 15 is 4 marks)**

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| **Qn** | **Answer** | **Mark** | **Notes** |
| --- | --- | --- | --- |
| **1(a)** | 429.8056 | 1 | P1 Process to work out the length of *AB*, e.g. *AB* = (29 – 14) ÷ sin 2 (= 429.8056….)  |
| **(b)** | 22.6 | 2 | P1 Process to work out Tom's speed, e.g. “429.8056” ÷ 19 A1 22.6(213...)  |
| **2\*(a)(i) and (ii)** | (3,4) and (6,1) | 1 | P1 Process to find the midpoint *M* or the midpoint of *AC*, e.g. or (3,4) and or (6,1) |
| **(b)** | 1 and −1 | 2 | P1 Process to find the gradient of *AC*, e.g.  (= 1)P1 Process to find the gradient of line joining *M* to the midpoint of *AC*, e.g.  (= −1) |
| **(c)** | A correct comment with working | 1 | C1 A correct comment eg since gradient of *AC* × gradient of line joining *M* to the midpoint of *AC* = −1, the lines are perpendicular so *L* passes through the midpoint of *AC* |
| **3\*(a)** | (2*x* – 3)2 – 4 | 1 | P1 Process to find gf(*x*), e.g. (2*x* – 3)2 – 4  |
| **(b)** | 4*x*2 − 12*x* + 5 | 1 | P1 Process to simplify gf(*x*) into the form *ax*2 + *bx* + *c*, e.g. 4*x*2 − 12*x* + 9 − 4 (= 4*x*2 − 12*x* + 5) |
| **(c)** | 4(*x* –  )2 – 4 | 2 | P1 Process to express gf(*x*) in the form *p*(*x* + *q*)2 + *r*, e.g. 4[(*x* –  )2 – 9/4] + 5 e.g. 4(*x* – )2 – 9 + 5 A1 4(*x* – )2 – 4 oe |
| **(d)** | ( , −4) | 1 | B1 (“” , “−4”) |
| **4(a)** | 1.2*x* | 1 | P1 Process to find the number of sausage rolls sold on Saturday, e.g. 1.2 × *x* (= 1.2*x*) |
| **(b)** | 0.9*x* | 1 | P1 Process to find the number of sausage rolls sold on Sunday, e.g. 0.75 × “1.2*x*” (= 0.9*x*) |
| **(c)** | 0.9*x* = 81 | 1 | P1 Process to set up an equation for the number sausage rolls sold on Sunday, e.g. 0.9*x* = 81 or *x* = 81 ÷ 0.9 (= 90) |
| **(d)** | 279 | 1 | A1 279 |
| **5\*(a)** | *c* = 18 | 2 | P1 Process to work out the value of *c*, e.g. 10 = −4(2) + *c* A1 for *c* = 18 |
| **(b)** | *a* = 2 | 2 | P1 Process to work out the value of *a*, e.g. *a* = −4(4) + “*c*” A1 for *a* = 2 |
| **6\*(a)(i) and (ii)****(b)** |  and  and  | `1 | P1 Process to find the proportion of rotten red apples or rotten green apples of the total number of apples, e.g. and  |
| **(c)(i) and (ii)** | + = 35 | 1 | P1 Process to set up the equation of the proportion of rotten red apples and rotten green apples, e.g. + = 35 |
| **(d)** | 200 | 2 | P1 Process to solve the equation, e.g. 20*x* + 8*x* = 35 × 8 × 20A1 |
| **7(a)** | 11.8758 | 1 | P1 Process to start to find the radius of the sector substitute correct values into equation of area of sector of circle, e.g. *π* × *r*2 × = 80 |
| **(b)** | 74.305° | 1 | P1 Full process to find the radius, e.g. *r* =  (= 11.8758)  |
| **(c)** | 46.056 | 2 | P1 Process to find an angle in triangle *ABE* or triangle *DCE*, e.g. A = cos-1 = (74.305°) P1 Process to work out the area of triangle *ABE* or triangle *DCE*, e.g. 0.5 × 10.4 × 9.2 × sin “74.305” (= 46.056) |
| **(d)** | 92.(1...) | 1 | A1 92.(1...) |
| **8(a)** | 7.6394 | 1 | P1 Process to find the radius or diameter of the tin, e.g. 2π*r* = 24 or πD = 24 |
| **(b)** | 3.8197 | 1 | P1 Process to find the radius of the tin, e.g. r = 24 ÷2π (= 3.8197……..) or *r* = D ÷ 2 = (24 ÷ π) ÷ 2 |
| **(c)** | 504 cm3 | 2 | P1 Process to find the volume of the tin, e.g. V= π × (“3.8197…”)2 × 11A1 504 cm3 (must have units) |
| **9\*(a)** | 8 : 6 : 21 | 2 | `P1 Process to combine the ratios by using a common multiple, e.g. (4 : 3) × 2 and (2 : 7) × 3P1 A complete process to combine the ratios, e.g. 8 : 6 : 21 |
| **(b)** | 72 and 189 | 1 | P1 Process to find the number of red counters and blue counters, e.g.  × 315 (= 72) and  × 315 (= 189) |
| **(c)** | 117 | 1` | A1 for 117 |
| **10\*(a)(i) and (ii)** |  and  | 1 | P1 Process to find length *AD* and *EH* ,e.g.  and  |
| **(b)** |  +  = 8 | 1 | P1 Process to set up an equation, e.g.  +  = 8 |
| **(c)** | 8*x*² − 3*x* − 5 = 0 | 1 | P1 Process to reduce the equation to a*x*² + b*x* + c = 0 e.g. 8*x*² − 3*x* − 5 = 0 oe  |
| **(d)** | 8*x* + 5)(*x* − 1) = 0 | 1 | P1 Process to solve quadratic equation, e.g. (8*x* + 5)(*x* − 1) = 0 |
| **(e)** | *AD* = 2 and *EH* = 6 | 2 | P1 Process to find length *AD* or *EH*, e.g.  or A1 *AD* = 2 and *EH* = 6 (clearly identified) |
| **11(a)** | 14.899 | 2 | P1 Process to find the length *BD*, e.g. 242 + 172 – 2(24 × 17 × cos38) (= 221.983)P1 A complete process to find the length *BD*,e.g.  (= 14.899) |
| **(b)** | 12.67682 | 1 | P1 Process to find the length *AD* e.g. *AD* =  × sin 56 (= 12.67682) |
| **(c)** | 69.1 | 2 | P1 Process to find the area of triangle *ABD*, e.g.  × “14.899” × “12.67682” × sin 47 (= 69.1)A1 for 69.1 |
| **12(a)** | 65*v* | 2 | P1 Process to work out the area of a section under the curve e.g. (60 − 20)*v* (= 40*v*) or (0.5)(20 − 0)*v* (= 10*v*) or(0.5)(90 −60)*v* (= 15*v*) P1 Process to work out the total area under the curve, e.g. "40*v*" + "10*v*" + "15*v*" (= 65*v*) |
| **(b)** | 65*v* = 2080  | 1 | P1 Process to find *v*, e.g. "65*v*"= 2.08 e.g. "65*v*"= 2080  |
| **(c)** | 32 | 1 | A1 for 32 |
| **13\*(a)** | 5*n* + 35 | 2 | P1 Process to set up an algebraic expression for the T-shape, e.g. *n* + *n* + 1 + *n* + 2 + *n* + 11 + *n* + 21 P1 Process to simplify the algebraic expression, e.g. 5*n* + 35 |
| **(b)** | 5(*n* + 7) | 1 | C1 for 5(*n* + 7) or equivalent explanation  |
| **14\*(a)****(b)** | 9 and 9*x*2 + 2*x* +1and 3*x* + 3 | 1 | P1 Process to work out the area of *JCFG* and *ABCJ* e.g. (*x* + 1)(*x* + 1) (= *x*2 + 2*x* +1) and 3(*x* + 1) (= 3*x* + 3) |
| **(c)** | *x*2 + 5*x* – 66 = 0 | 2 | P1 Process to set up an equation for the area of the shape, e.g. “*x*2 + 2*x* +1” + “3*x* + 3” + “18” = 88 P1 Process to simplify the quadratic equation into the form *ax*2 + *bx* + c = 0 e.g. “*x*2 + 5*x* – 66 = 0” |
| **(d)** | 6 | 2 | P1 Process to solve the quadratic equation, e.g. (*x* + 11)(*x* – 6) = 0A1 for *x* = 6 |
| **15\*(a)****(b)** | 4*h* |  |  |
| **(c)(i)** | *h* = 8 | 1 | P1 Process to set up an equation, e.g. *h* = 2 × “4” |
| **(c)(ii)** |  | 1 | P1 Process to rearrange for *h*, e.g. *h* =  |
| **(d)** |  | 2 | P1 Process to rationalise the denominator, e.g. *h* =A1 for (Accept *a* = 8 and *b* = 1) |